

o y $*$ conmutan: $(a o b) * (c o d)$

$$\begin{aligned} & 1_o \text{ neutro de } o \quad 1_* \text{ neutro de } * \quad o \text{ y } * \text{ conmutan} \quad 1_o \text{ neutro de } o \quad \text{asociatividad} \\ 1_o &= 1_o o 1_o = (1_o * 1_*) o (1_o * 1_*) = (1_o o 1_o) * (1_* o 1_*) = 1_o * (1_* o 1_*) = \\ & (1_o * 1_*) o 1_* = 1_o o 1_* = 1_* \text{ neutro de } o. \text{ Entonces } \boxed{1_o = 1_*} \end{aligned}$$

$$a * b =? a o b$$

$$\begin{aligned} & 1_o \text{ neutro de } o \quad o \text{ y } * \text{ conmutan} \quad 1_o = 1_* \quad 1_* \text{ neutro de } * \\ a * b &= (a o 1_o) * (1_o o b) = (a * 1_o) o (1_o * b) = (a * 1_*) o (1_* * b) = a o b \end{aligned}$$

Entonces $\boxed{a * b = a o b}$

$$a * b =? b * a$$

$$\begin{aligned} & 1_o \text{ neutro de } o \quad o \text{ y } * \text{ conmutan} \quad 1_o = 1_* \quad 1_* \text{ neutro de } * \\ a * b &= (1_o o a) * (b o 1_o) = (1_o * b) o (a * 1_o) = (1_* * b) o (a * 1_*) = b o a \\ & = b * a \end{aligned}$$

Entonces $\boxed{a * b = b * a}$